

Parallelizing a Computationally Intensive Financial R Application with Zircon Technology

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Abstract

Statisticians, analysts, scientists, and engineers require massive processing power to conduct data analysis, predictive modeling, visualization, and other complex tasks. This paper describes how we substantially improved the performance of a representative complex computational finance application by integrating the Zircon adaptive ultra high-performance computing software platform and tools with the R programming language and environment. This integrated solution uses distribution and parallelization to reduce the total computation time of the R-based application from 3,093 minutes to 39 minutes on a commodity multi-processing platform containing 80 cores and from 2,217 minutes to 22 minutes in a high-performance cloud environment containing 104 cores.

1 Introduction

Companies in competitive domains, such as financial services, digital media, text mining, and enterprise content management, create large data repositories containing large amounts of data collected from their daily operations. Analyzing this archived data can yield knowledge that drives future business and provides significant market advantages over competitors. Although companies could use specialized super computers, the custom development time and hardware costs are prohibitive.

Another approach is to use proprietary, and custom built high-performance computing (HPC) software platforms, such as MPI [9], PVM [6, 8], OpenMP [10], or Globus [5], atop multi-core/multi-node platforms. This approach has the following drawbacks:

- **Price-per-core performance is not tied to linear gains in application speedups or compute process-**

ing. Conventional HPC software and hardware platforms are cost-prohibitive since they do not accelerate performance commensurately to the investment of resources allocated and do not adapt dynamically to changing workloads and resource availability.

- **Custom development and integration.** Conventional HPC software platforms require extensive manual development and integration of custom server and application programming before they can work (and many common and legacy apps cannot be modified unless they are redeveloped).
- **Tied to modified apps.** Once applications are customized, they are locked in to a particular HPC platform and deployment configuration, and cannot leverage updates without redoing the intense customization.
- **Complex setup with no support for automated plug and play.** Conventional HPC software platforms require complex setup and customization to adjust the load manually on all processors in the network since they don't have automatic adaptive load balancing.

This paper describes how we overcame the limitations with conventional HPC platforms to substantially improve the performance of a representative complex computational finance application—the Garrett Asset Management Backtesting System—by integrating R [11] and Zircon software [1]. R is a programming language and software environment for statistical computing and graphics that provides rich platform support for data modeling, analysis, and visualization. Zircon is an adaptive ultra high-performance computing software platform and tools that requires no server development; minimal application integration; is easy and automatic to setup; and scales quickly from a few laptops to tens of thousands of multi-core servers ranging from multi-core, LANs, WANs, and clouds.

The Garrett Asset Management (GAM) Backtesting System financial application uses historical and hypothetical simulations to assess mathematical models used to drive high-frequency electronic trading and help inform complex decision-making. Like many financial applications, the GAM Backtesting System executes a large number of logically independent and computationally intensive calculations to simulate the behavior of various algorithms on historical data. For example, the GAM Backtesting System executes a large number of financial models over a sequence of historical time periods that may also be large. For each combination of a model and a time period, the GAM backtesting system performs the same computationally intensive calculation and collects results until computations are performed for all the models over all the time periods.

R was a natural choice to meet GAM's statistical analysis requirements since its convenient abstractions allow statisticians and engineers to run complex data analysis with a few commands. R's interpretive structure, however, was a limiting factor for delivering complex and mission-critical analysis in a timely fashion. Integrating R with Zircon software thus allowed users to focus on writing their application logic related to data modeling, analysis, and visualization in the intuitive R language while leaving the complexities of accelerating computation-intensive R applications to Zircon software's adaptive ultra high-performance computing solution.

The remainder of this paper is organized as follows: Section 2 describes the limitations of applying traditional parallel computing solutions to accelerate compute-intensive R applications, such as the GAM Backtesting System; Section 3 describes the structure and functionality of the Zircon software; Section 4 describes how we used Zircon software to parallelize and accelerate the complex compute-intensive calculations of the GAM Backtesting System; Section 5 analyzes empirical results that demonstrate the performance improvements after parallelizing the sequential GAM Backtesting System using Zircon software; and Section 6 presents concluding remarks and lessons learned.

2 Strategies and Challenges for Accelerating Compute-Intensive R Applications

R is a statistical software package that provides analysts with a comprehensive environment for statistical computation, data manipulation, data analysis, and graphical data visualization. It provides a full-fledged statistical language with first-class support for performing operations on complex data structures such as arrays and matrices. R also provides many libraries and packages for performing complex statistical operations and assisting analysts in varied domains including finance, econometrics, clinical trials, machine and statistical learning, natural language processing,

and genetics [7].

With the proliferation of R in various domains requiring complex data analysis tools, several strategies have emerged to accelerate R applications. For example, custom analytic routines and libraries can be written in compiled languages, such as C and C++, and run within the R environment to accelerate analysis and enhance reuse, thereby saving significant development time and effort. To facilitate this integration, the *Rcpp* [4] and *RInside* [3] packages can be used to seamlessly integrate R code into C/C++ applications. Another strategy involves performing complex calculations in parallel across multiple processors to deliver results quickly and scalably. For example, R has been integrated with *Rmpi* [17] and *snow* [16] to distribute calculations over many computers.

These existing strategies for accelerating complex R applications however, incur the following challenges:

- Integration technologies, such as *Rcpp*, are effective for accelerating computations within a single processor by replacing interpreted R code with efficient compiled code. These integration technologies, however, cannot easily perform complex calculations and analysis in parallel across multiple computers in a cloud environment.
- Existing parallel computing solutions [12] for R are based on conventional grid computing middleware, which is cumbersome to program for the reasons described in Section 1. As a result, significant amounts of time and effort must be spent studying tutorials, webinars, and other materials to educate developers on these hard-to-program technologies.

What is needed, therefore, is a solution that can leverage both hardware and software innovations in distributed and parallel computing, while simultaneously reducing the learning curve and effort needed to incorporate these innovations into mission-critical applications. In particular, an ideal solution should allow data analysts to (1) easily distribute complex calculations/analysis across multiple processors and execute them in parallel, (2) invoke analysis routines in compiled and/or interpreted languages seamlessly on any OS/hardware platform, and (3) improve runtime performance via advanced hardware technologies (*e.g.*, using massive and elastic cloud processing capabilities) and software technologies (*e.g.*, by switching between R and compiled code as needed).

3 Solution Approach: Integrating R with the Zircon Software

The Zircon Software Product Suite [1] from Zircon Computing provides an adaptive ultra high-performance

computing middleware platform that substantially accelerates the performance of R applications and addresses the challenges with existing strategies described in Section 2. Zircon software automatically deploys a distributed computing infrastructure across heterogeneous or homogeneous hardware platforms and operating systems, maps compute-intensive applications to a pool of processors, manages their execution, and dynamically equalizes the workload in real time to fit available resources. Application developers can thus exploit the processing power available to them, including newer technologies, such as multi-core processors and cloud computing systems, as well as traditional desktops and servers.

3.1 Features and Benefits of Zircon Software

Below we describe the key features and benefits of Zircon software.

3.1.1 Extreme Performance that is Cost Effective

Zircon provides a cost-effective adaptive ultra high-performance computing solution via the following features:

- **Real-time load equalization.** Zircon utilizes and distributes the workload in real-time across all available computing and networking resources, including multi-core desktop, LAN, WAN or any accessible cloud network. This load equalization ensures every processor in the grid is optimized to maximize computing performance.
- **Transparent scalability.** Processors and cores can be added or removed (and allocated for other tasks) without disrupting ongoing operations since Zircon software automatically recognizes the state of the processors and allocates workload without changing application software.
- **Distributed data caching.** Zircon software can cache large data structures on servers by sending the data just once, then sending a reference to the cached data on each server during each request. This distributed data caching accelerates distributed applications where communications overhead is significant compared to the actual computation time.
- **Ultra-fast data transfer.** Unlike conventional middleware, that bottlenecks application data between clients and servers by using text-based protocols (*e.g.*, HTML, XML, and SOAP), Zircon software automatically generates optimized binary protocols that transfers results much faster.

- **No virtualization overhead.** Zircon software runs at native operating system speeds on heterogeneous operating systems, hardware platforms, programming languages, and network environments with no virtualization overhead.

3.1.2 Minimal Development Effort

Zircon minimizes the time to develop HPC applications via the following features:

- **No server-side development.** Unlike competing HPC platforms, Zircon can execute existing application functions and algorithms in parallel without requiring any server-side development. This capability allows quicker development and can utilize existing servers including those within the cloud. Conventional HPC software platforms cannot be used in cloud computing—since external data centers would not want you tampering with their servers.
- **Minimal application development.** Zircon software is designed as a component-based framework that contains many “knobs” can be extended and tuned transparently to easily and quickly support new user requirements and application feature enhancements.
- **Maintains application security.** Zircon software does not need to know the application data and sensitive business logic to operate, which means it is always secure and confidential.

3.1.3 Rapid Configuration and Deployment

Zircon minimizes the time to configure and deploy HPC applications via the following features:

- **Automatic parallel configuration.** Zircon includes asynchronous adapters that quickly configure existing non-parallel application code to run in parallel execution that run much faster by leveraging the processing power of the entire grid. These adapters can also configure applications to run in collocated and/or distributed parallel deployments that maximize the use of available computing resources.
- **Platform independence.** Any distributed and/or collocated computation can be deployed on any popular operating system or platform with complete and automatic interoperability. This platform independence means a Windows application can leverage the processors on Linux, Solaris, AIX, Mac, and other operating systems without having to re-write or port the applications themselves since Zircon handles the conversions automatically.

3.1.4 Intuitive Use and Administration

The following features make Zircon intuitive to use and administer:

- **Automatic load equalization.** Unlike conventional HPC software platforms, Zircon software automatically equalizes the load between all of the available (heterogeneous and/or homogeneous) processors in the grid adaptively, which eliminates the tedious trial and error needed to maximize performance.
- **Automatic service discovery.** Zircon software dynamically discovers and optimizes all processors available at runtime. When new machines are added or removed from a deployment, Zircon software will automatically reconfigure accordingly, which ensures maximum performance at all times with little or no administrative input.
- **Automatic real-time monitoring and auditing.** Zircon software provides powerful tools for automatically monitoring and transparently auditing huge volumes of application and system events. These tools minimize the total cost of ownership by enabling real-time decision making that is more accurate and relevant than is possible with manual monitoring and current auditing approaches.
- **Persistent and recoverable.** Zircon software uses an adaptive, fault-tolerant architecture that ensures that applications will automatically recover and transparently re-execute requests on different servers if existing servers disconnect or fail.

3.2 The Zircon Software Architecture

Applications built using Zircon software are known as *zEnabled* applications. Zircon software supports three computing and communication models required by many mission-critical *zEnabled* applications that need ultra high performance, as shown in Figure 1 and described below:

- **Application executable parallelism**, such as the capabilities provided by data centers and clouds to launch applications on demand. The *zExec* application execution parallelism service runs any executable in a cluster of servers as a set of parallel jobs, thereby simplifying coarse-grained application parallelization.
- **Application function parallelism**, such as the capabilities provided by computation grids to run application operations in a cluster of servers as if they were programmed for a single computer. The *zFunction* function parallelism API and supporting tools hide many low-level network programming concerns and

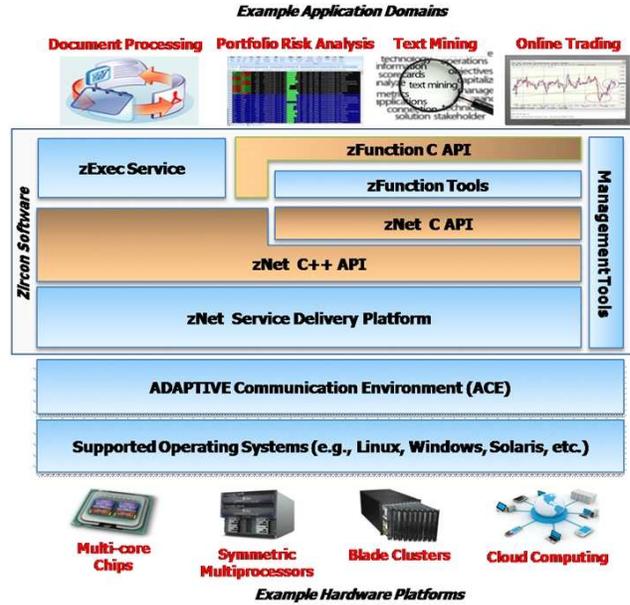


Figure 1: Zircon Software Architecture

unexpected complexities, simplifying finer-grained application parallelization.

- **Service delivery platforms**, such as the capabilities provided by distributed computing environments that support fine-grained cooperating business tasks via distributed infrastructure patterns [2], such as *Messaging*, *Broker*, and *Publisher/Subscriber*. The *zNet* API provides a C++ interface to the *zNet* service delivery platform that handles service discovery, reliable multicast communication, request load balancing, and request dispatching.

Requests from applications that use these three models can run on processors and cores in a collocated and/or distributed manner, with the choice of collocation or distribution largely transparent to application clients and servers. Zircon software runs on all popular general-purpose and real-time operating systems since it is implemented atop the open-source ADAPTIVE Communication Environment (ACE) [13, 14]. ACE is portable C++ host infrastructure middleware that shields Zircon software from operating system dependencies without incurring the overhead of hypervisor-based virtualization mechanisms.

4 A zEnabled-R Solution for the GAM Back-testing System

This section describes how we used the Zircon *zNet* service delivery platform described in Section 3.2 to parallelize

and accelerate the complex compute-intensive calculations of the GAM Backtesting System described in Section 1. We first describe the structure of a typical zEnabled R application and then describe how we used this structure to accelerate GAM Backtesting System performance.

4.1 Structure of a Typical zEnabled R Application

zEnabled R applications follow the general Zircon software paradigm of having a client application invoke multiple asynchronous requests on remote compute servers (Figure 2, Steps 1 and 2) through Zircon’s dynamic real-time load equalizer (which resides within the zNet Client Middleware shown in Figure 2). Parallelization is achieved by

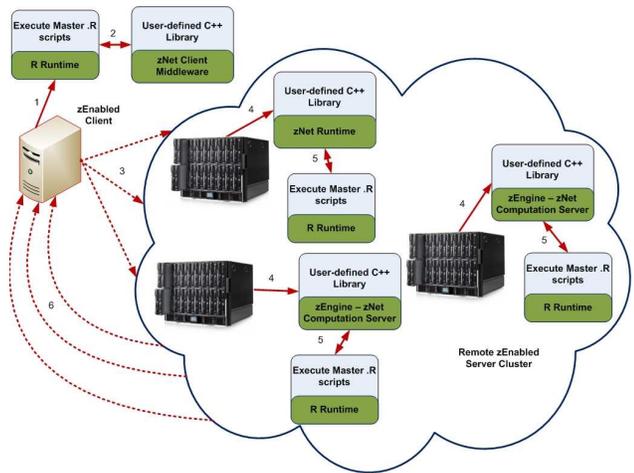


Figure 2: The Structure of a Typical zEnabled R Application

executing these requests in parallel on multiple generic Zircon compute servers, known as zEngines (Figure 2, Step 3). As soon as each computation completes its results are returned to the client application (Figure 2, Step 6). The request and results are performed in one function call that is synchronous from the perspective of R client applications, i.e., remote computation results are available for use by a client after all results of parallel computations are returned.

The zEnabled client application consists of R code that loads Zircon software as a plug-in library via the Component Configurator pattern [15]. Likewise, the server application dynamically loads the R language library and user-defined R functions into a zEngine process, which provides a lightweight container for zEnabled software (Figure 2, Steps 4 and 5). To execute R code, the zEngine loads both the R language interpreter library and application-specific R definitions for functions that will process requests received from clients in parallel with other requests.

Zircon software on the client and server(s) uses a compact, application-specific binary protocol to transmit re-

quests and results. This protocol is implemented via (de)serialization operators for user-defined C/C++ types. The interface between the user’s R code and Zircon software therefore requires defining mappings between native R data types and serializable C++ objects for each R function with a distinct signature. These mappings are provided by a user library that can be written using Zircon APIs and tools.

To simplify the development of user libraries for R integration, Zircon software provides the zNet-R component, which wraps an instance of the R interpreter implemented as a RInside object. RInside and its associated Rcpp package provide a facade for accessing and manipulating native R types from within a C++ application. Developers of user libraries can use these utilities to efficiently map types used by R to/from serializable C++ objects, such as STL vectors and strings. In particular, the Rcpp package allows users to serialize diverse R types, such as values, vectors, matrices, and data frames.

4.2 Implementing a Parallelized Garrett Asset Management (GAM) Backtesting System

Figure 3 compares and contrasts the original sequential GAM Backtesting System with the corresponding zEnabled parallelized version. Figure 3a shows how the original application contains two nested loops that iterate over a number of financial models (the MODELS list) and a large set of points in a multi-dimensional parameter space (StratPars). The bulk of the calculation is performed by the GenericgetNAVs() function that simulates a particular model with a set of parameters drawn from this space. The parameter space is large and may have any number of dimensions, with typical runs totaling nearly 100,000 distinct invocations. Most of these invocations are homogeneous, taking several seconds to complete on commodity hardware.

The parallel zEnabled implementation shown in Figure 3b is structurally similar to the sequential code. For example, both the sequential and parallel implementations meet the post-condition that the allres matrix has been completely populated with results at the end of the loops. Likewise, both implementations iterate over a number of objects in the MODELS list and execute simulations with them. The key difference between the sequential and parallel implementations is that the nested loop in Figure 3a iterating over the points in a parameter space is replaced in Figure 3b with a single call to the call_get_navs() function, which interfaces application user library code with Zircon software.

The call_get_navs() function reproduces the behavior of the inner loop in Figure 3a by (1) dispatching asynchronous requests to remote zEngine compute servers, (2)

```

for (x in MODELS)
{
  DoBacktest (....)
  {
    BacktestAStrategy (.....)
    {
      CompleteSpace (.....)
      {
        for (l in 1:length (StratPars$x))
        {
          allres <- rbind (allres,
                          GenericgetNAVs (...))
        }
      }
    }
  }
}

```

(a) Pseudo Code of the Sequential Implementation

```

for (x in MODELS)
{
  DoBacktest (....)
  {
    BacktestAStrategy (.....)
    {
      CompleteSpace (.....)
      {
        // every iteration of the for loop
        // executed in remote servers
        // with independent data

        allres <- call_get_navs (...)
      }
    }
  }
}

```

(b) Pseudo Code after Parallelization with Zircon Software

Figure 3: **Different Implementations of the GAM Backtesting System**

awaiting the delivery of all results, and (3) populating the `allres` matrix. While each request is asynchronous—and thus may execute in parallel—the `call_get_navs ()` function is synchronous from an R application perspective. This routine is implemented as a lightweight R wrapper around a C++ function and uses `Rcpp` to map between native R types (such as the `allres` matrix and its constituent rows) and serializable C++ types (such as `std::vector<double>`). The performance boost delivered by the zEnabled parallel implementation shown in Figure 3b was dramatic, as shown next.

5 Analysis of Empirical Results

This section presents the results of the experiments that quantify the benefits of parallelizing and/or distributing the GAM Backtesting System application using zNet-R, which integrates the R interpreter and Zircon software. We ran the following two sets of experiments:

- The first set of experiments was conducted on our zLab testbed containing 20 Intel-Xeon 1520 dual-series dual-processor/dual-core (for a total of 80 cores) 1.86 GHz machines running on 64-bit Red-Hat Enterprise Linux 2.6 and connected using Gigabit Ethernet. To maximize the utilization of the available hardware we dedicated one core to run the client application and devoted the remaining cores (a maximum of 79 cores on 20 machines) to run zEngine computation servers.
- The second set of experiments was conducted on a IBM cloud environment containing 13 quad-processor/dual-core (for a total of 104 cores) 3.0 GHz machines running on 64-bit Red-Hat Enterprise Linux

2.6 and connected using Gigabit Ethernet. To maximize the utilization of the available hardware we again dedicated one core to run the client application and devoted all remaining cores (a maximum of 103 cores on 13 machines) to run zEngine computation servers.

We chose two different testbeds to demonstrate that the benefits of Zircon software are hardware independent, *i.e.*, it can provide ultra-high-performance application acceleration in a convenient and scalable manner.

5.1 zLab Testbed Results

The first set of experiments ran the distributed parallelized version of the GAM Backtesting System application on three, five, nine, seventeen, and twenty multi-core machines and compared the performance of the application in each of these configurations with the performance of the baseline sequential application implementation. Since each machine in the experiment contained four cores, we started four instances of the GAM Backtesting application server on each machine (except the machine that ran the client application) to leverage all the four cores in each machine. On the machine running the client application, one core was used to run the client application and three other cores were used to run the zEngine computation servers.

The results in Figure 4 show near-linear performance gain with respect to the number of cores used in each experiment configuration. In particular, the sequential application took 3,093 minutes to calibrate and analyze two models. Conversely, it took 39 minutes for the distributed parallel version of the GAM Backtesting System to process and to analyze the same two models, which is substantially faster.

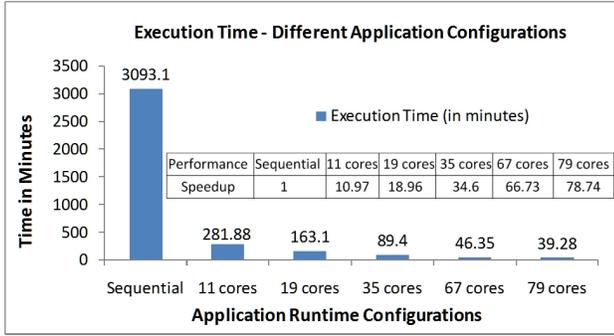


Figure 4: Performance of zEnabled GAM Backtesting System in zLab Testbed

The performance gains achieved by the distributed and parallel version of the GAM Backtesting System are limited only by the number of cores/machines available to run these experiments in our zLab testbed.

5.2 IBM Cloud Results

The new generation of clouds or datacenters with hundreds of machines and thousands of cores can devote more cores/machines to parallelize the GAM Backtesting System than we have in our zLab testbed. In such large-scale deployments, the GAM Backtesting System could be scaled transparently to utilize all the available cores and provide accelerations much higher than those shown in Figure 4. To demonstrate this scalability, we ran a second set of experiments on an IBM cloud environment using a distributed and parallel version of the GAM Backtesting System on one, two, three, and thirteen multi-core machines that are much more powerful than the hardware available in the zLab testbed.

To leverage all eight cores on each machine in the experiment, we started eight instances of the GAM Backtesting System application server on each machine (except the machine that ran the client application, where one core ran the client application and the remaining cores ran zEngine computation servers). The results of the experiments shown in Figure 5 again demonstrate near-linear performance improvement with respect to the number of cores used in each experiment configuration. These results show that sequential application analyzed two models in 2,217 minutes. Conversely, it took only 97 minutes for the distributed and parallel version of the zEnabled GAM Backtesting System to process and analyze two models across 23 cores. It took even less time (22 minutes) for the same zEnabled version to analyze the same two models across 103 cores.

Comparing Figure 4 with Figure 5 shows that GAM Backtesting System continues to achieve near-linear performance acceleration as the number of cores and the hardware

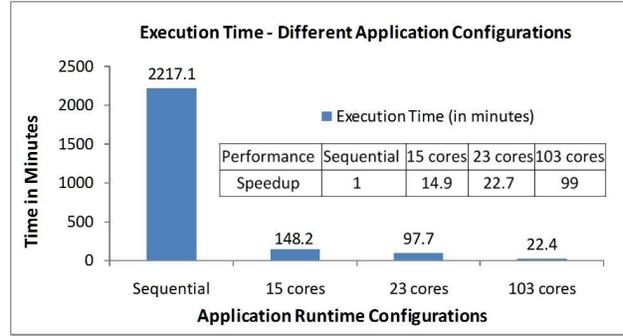


Figure 5: Performance of zEnabled GAM Backtesting System in IBM Testbed

capabilities increase. These results foreshadow the benefits of deploying the GAM Backtesting System across even larger-scale hardware deployments to obtain the adaptive distributed and parallel computing benefits of Zircon software.

6 Concluding Remarks

This paper demonstrated how the Zircon adaptive ultra high-performance computing platform has been integrated with the R programming environment to form zNet-R, which accelerates complex and compute-intensive R applications in the financial services domain. zNet-R dramatically improved performance with little learning curve and configuration/deployment effort. The results of our experiments showed how zNet-R accelerated the performance of the GAM Backtesting System significantly in several representative distributed and parallel computing environments.

Based on our experience parallelizing the GAM Backtesting System, the following are the advantages that R programmers would experience while parallelizing applications like the GAM Backtesting System:

- Programming with Zircon Software and the zNet-R middleware is straightforward and application developers are shielded from tedious and error-prone low-level network programming, distributed programming, and parallel programming. This advantage is significant for R users, who typically choose R to avoid wrestling with these low-level programming concerns. R users can thus focus on their application logic related to data modeling, analysis, and visualization, and leave the complex details related to distributed and parallel computing infrastructure to Zircon software.
- The acceleration benefits that R users derive from zNet-R middleware are not just restricted to R applications. For example, users could also distribute and/or parallelize analysis applications written in compiled

languages, such as C and C++, thereby providing an integrated environment for accelerating complex and compute-intensive applications developed in compiled and interpreted languages.

- Zircon software is extremely efficient and scalable in utilizing all the available processing cores of high-performance computing platforms, as shown in the linear acceleration obtained by the GAM Backtesting System. Moreover, Zircon software runs seamlessly over a wide range of computing platforms, including local-area networks; wide-area networks; public, private, or hybrid cloud deployments; and/or in dedicated data centers.

7 Participants

Zircon Computing. Zircon Computing, LLC, is an international software and services company based in Wayne, New Jersey. Founded in 2005 by senior technologists from the financial services industry, Zircon Computing is a leading provider of ultra high-performance middleware software and services worldwide, and markets both directly to enterprise clients and through an international network of partners. Zircon Computing is privately held. For more information, please visit <http://www.zircomp.com>.

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Garrett Asset Management. Garrett Asset Management, LLC, is a systematic trader in the financial and commodity futures. The firm was founded in 2009 with emphasis in research in portfolio construction, position sizing, and the development of technical trading models for different market conditions. For more information, please visit <http://www.garrettassetmanagement.net>.

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